

Efficient 2-D Integral Equation Approach for the Analysis of Power Bus Structures With Arbitrary Shape

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Introduction

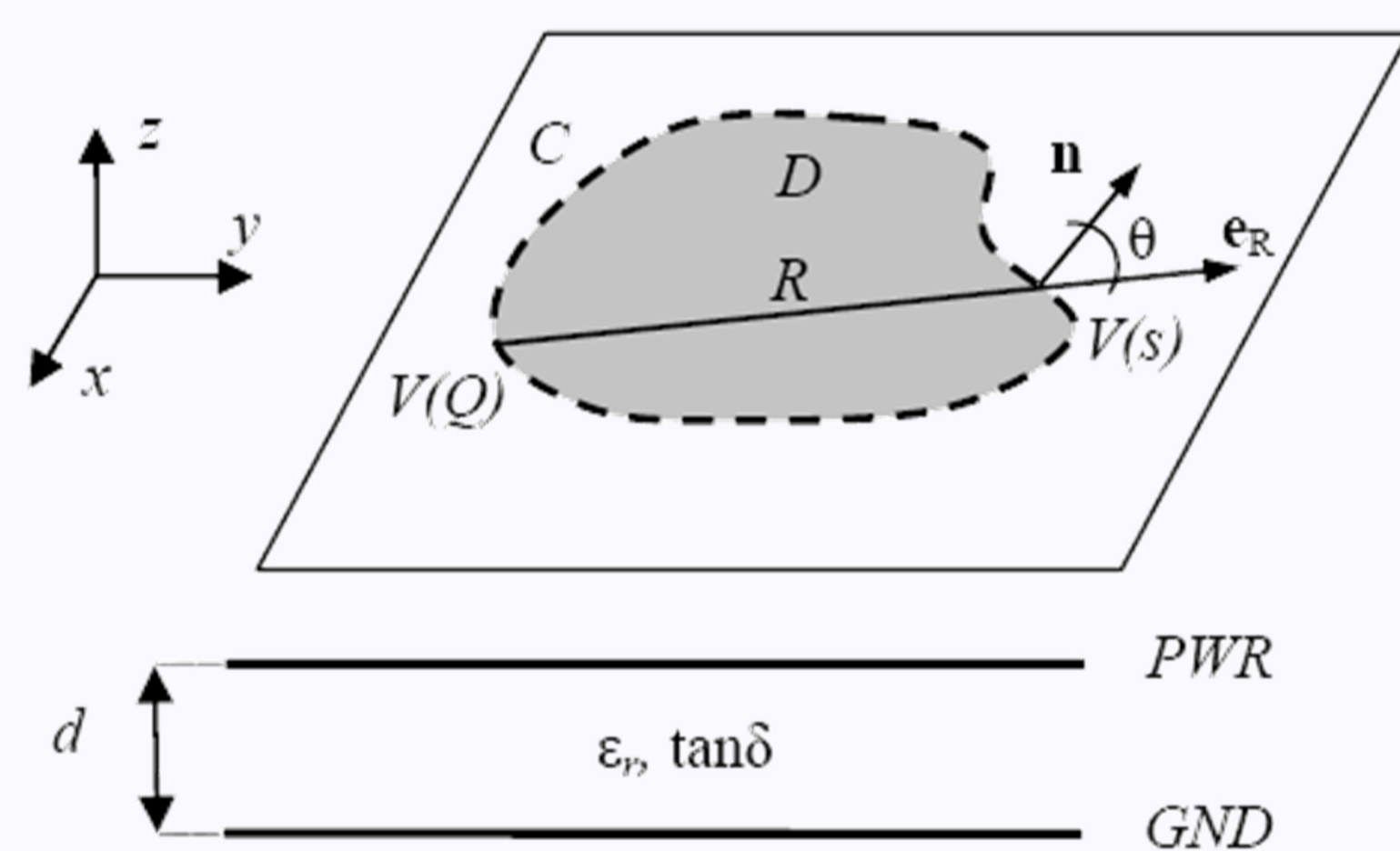
- Design objective for power-bus structures in multilayer printed-circuit board (PCB): Sufficient charge storage for fast switching integrated circuits (ICs)
 - ⇒ reduction of the switching noise
 - ⇒ ensuring power- and signal integrity
 - ⇒ minimizing radiated emissions
- Required efficient numerical analysis to determine:
 - voltage distribution between power/ground planes
 - voltage/current relations between the ports
 - electromagnetic emission

2D Contour Integral Formulation

- Weber's solution for cylindrical waves in terms of the boundary voltage $V(Q)$:

$$V(Q) = \frac{1}{2j} \oint_C [k H_1^{(2)}(kR)V(s) \cos\theta - j\omega\mu_0 d H_0^{(2)}(kR)i_{sn}(s)] ds$$

Problem configuration

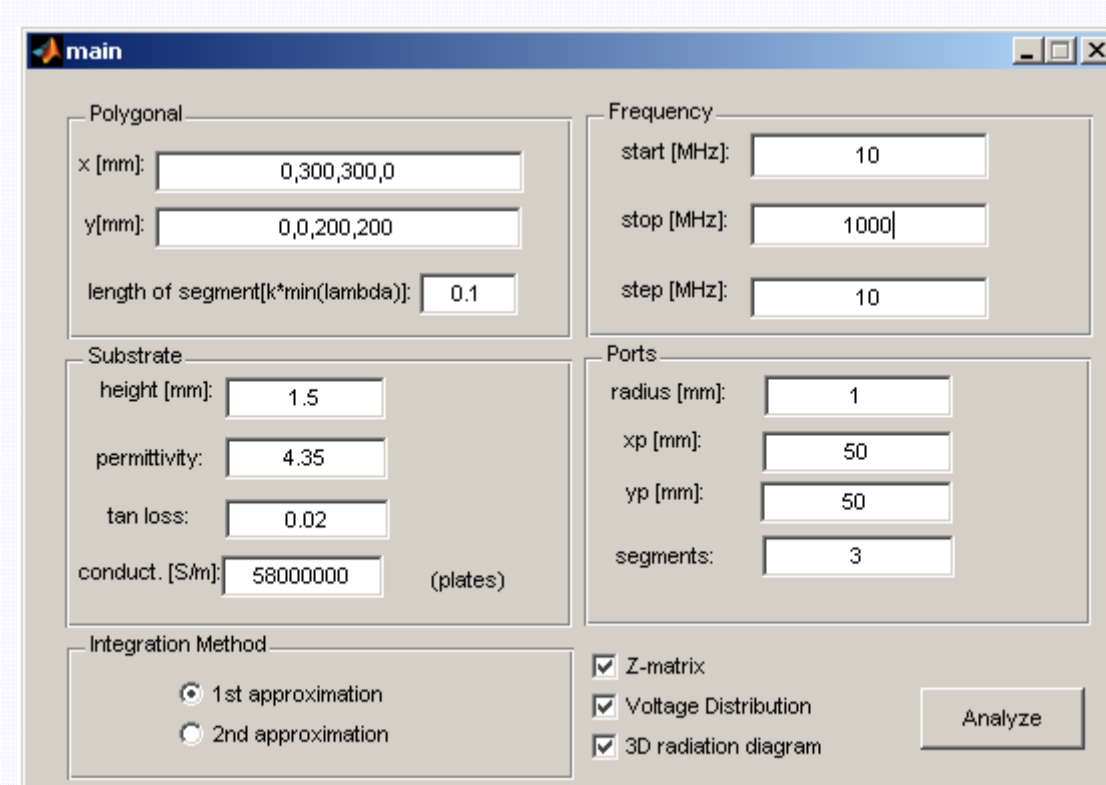


Advantages in comparison with conventional 3D modeling:

- Reduction of the problem dimension (3D → 2D)
 - ⇒ simple input of geometry for arbitrary polygonal shape
 - ⇒ small number of unknowns
 - ⇒ low CPU and memory demands
- Rapid calculation of frequency-dependent transfer characteristic for multiple ports

Numerical Implementation

User interface of the Matlab® program



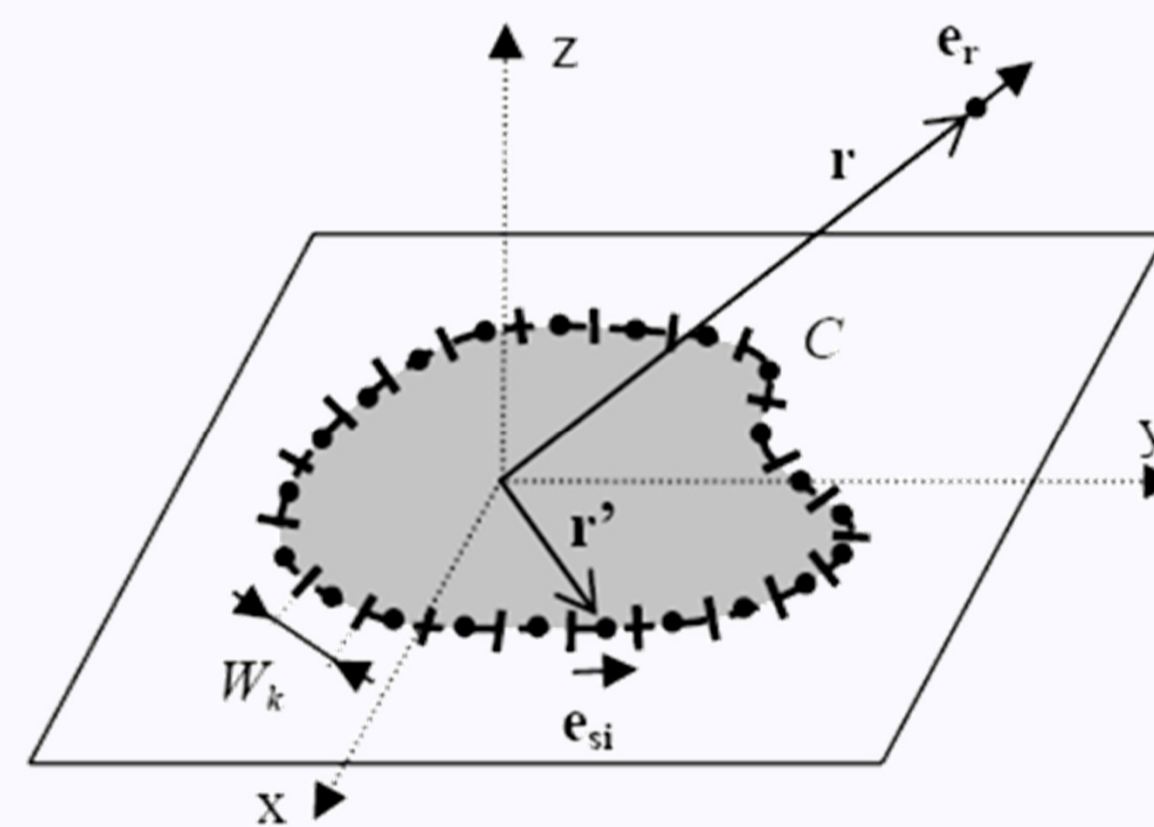
Voltage distribution $V(x,y)$ and far-field radiation characteristic

- Proper choice of the placement of critical ICs
- Calculation of radiated fields, based on the field equivalence principle

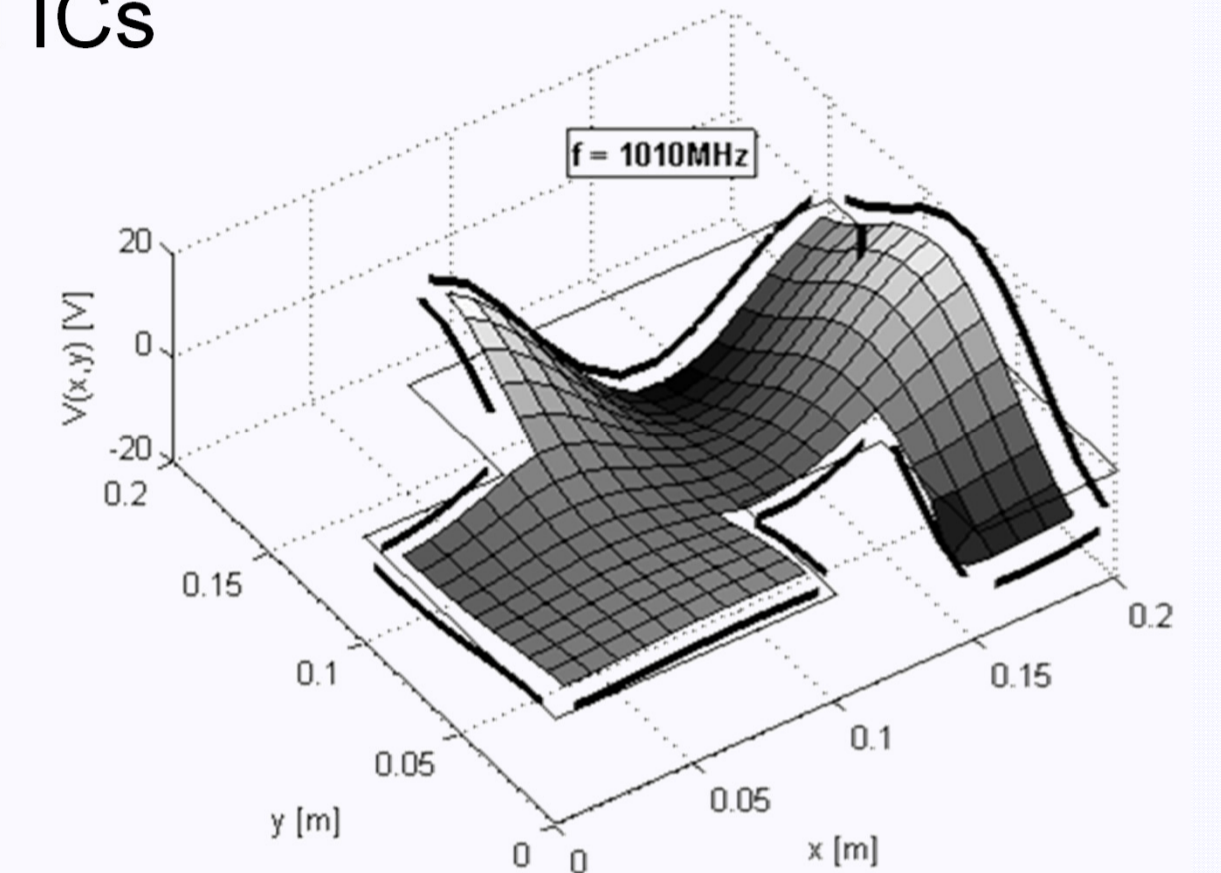
$$\mathbf{E}(\mathbf{r}) = \frac{jk_0 d}{4\pi r} \int_C M_S(\mathbf{r}') e^{jk_0 \mathbf{r}' \cdot \mathbf{e}_r} (\mathbf{e}_r \times \mathbf{e}_s) ds$$

Equivalent magnetic current:

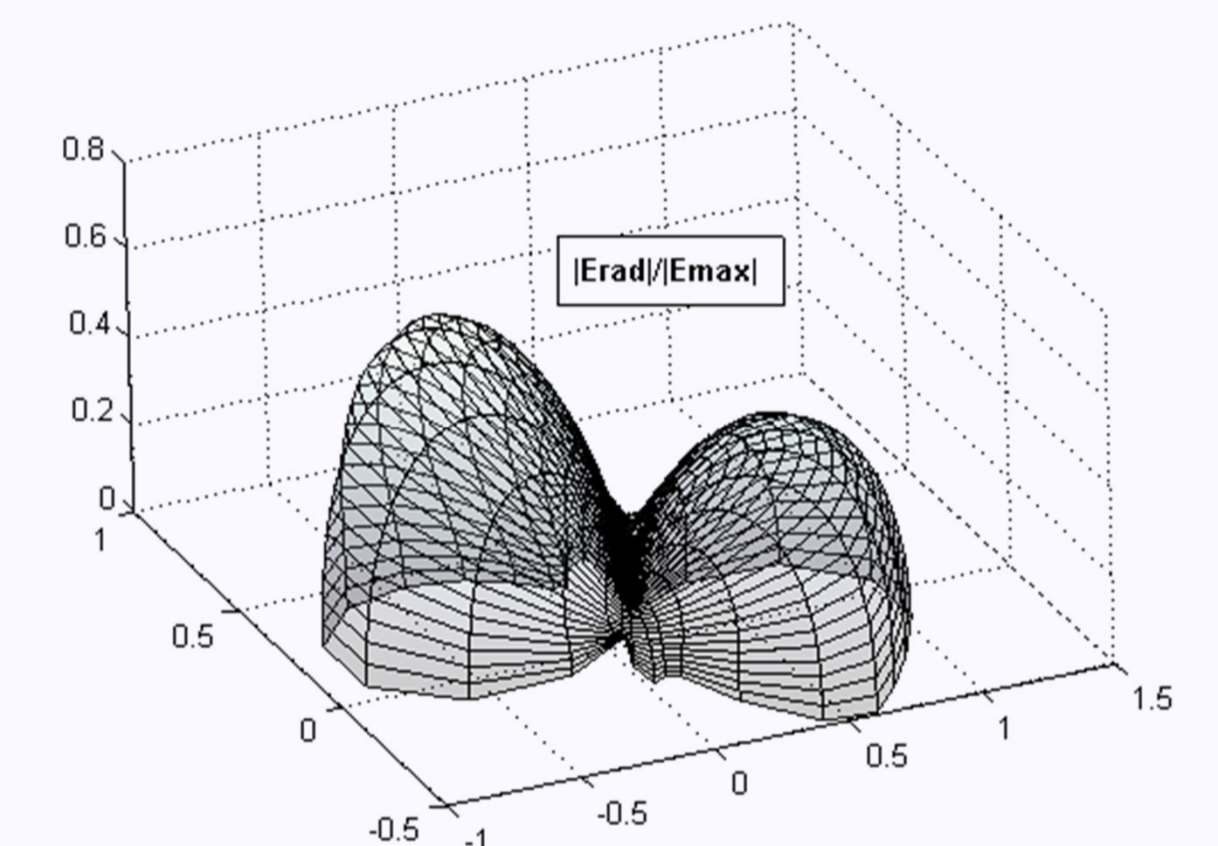
$$\mathbf{M}_S = -\mathbf{n} \times \mathbf{E} = \frac{V(s)}{d} \mathbf{e}_s$$



Numerical evaluation of radiated far fields

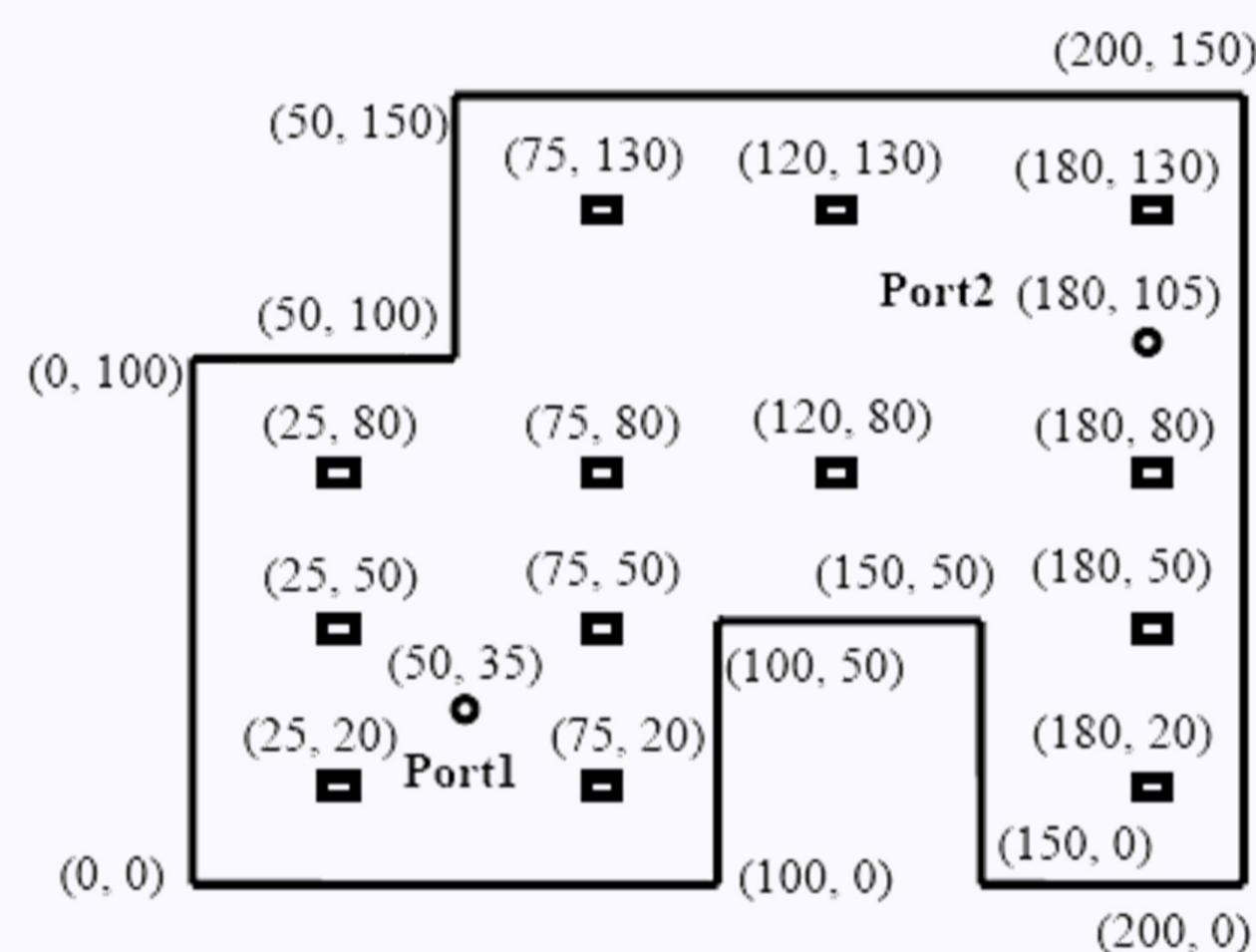


Voltage distribution within a power-bus

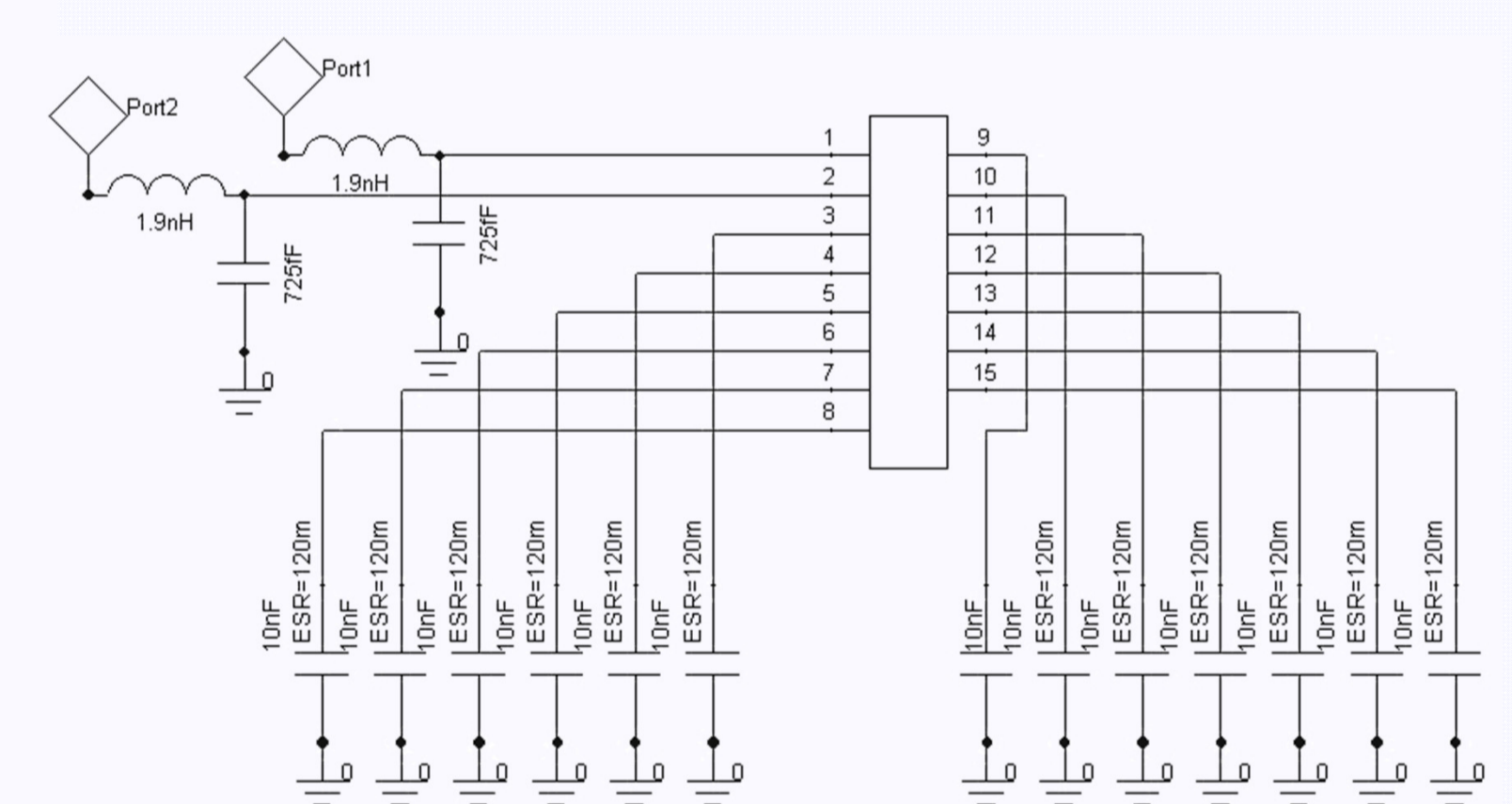


Radiation characteristic @ 1010 MHz.

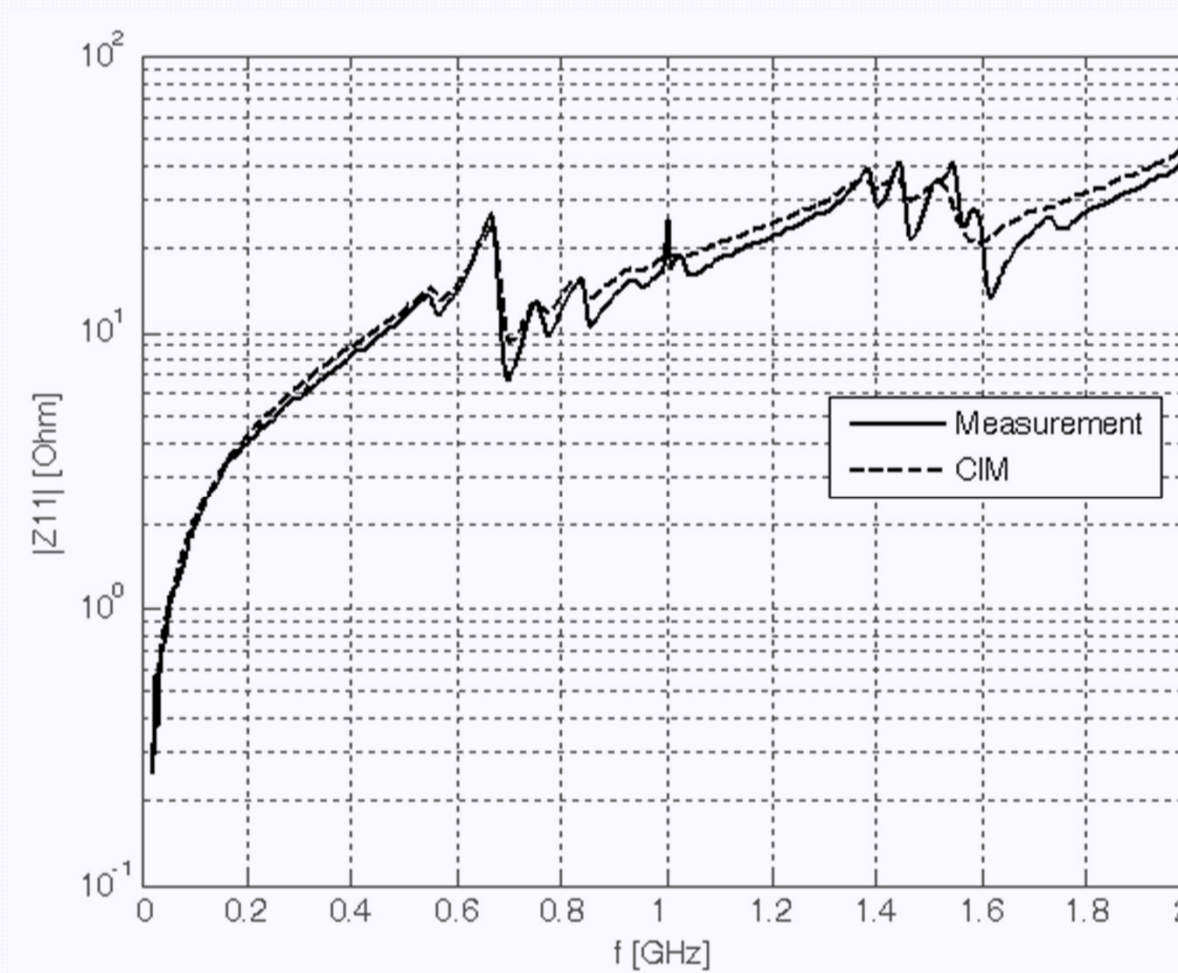
Experimental validation by measurement of populated PCB



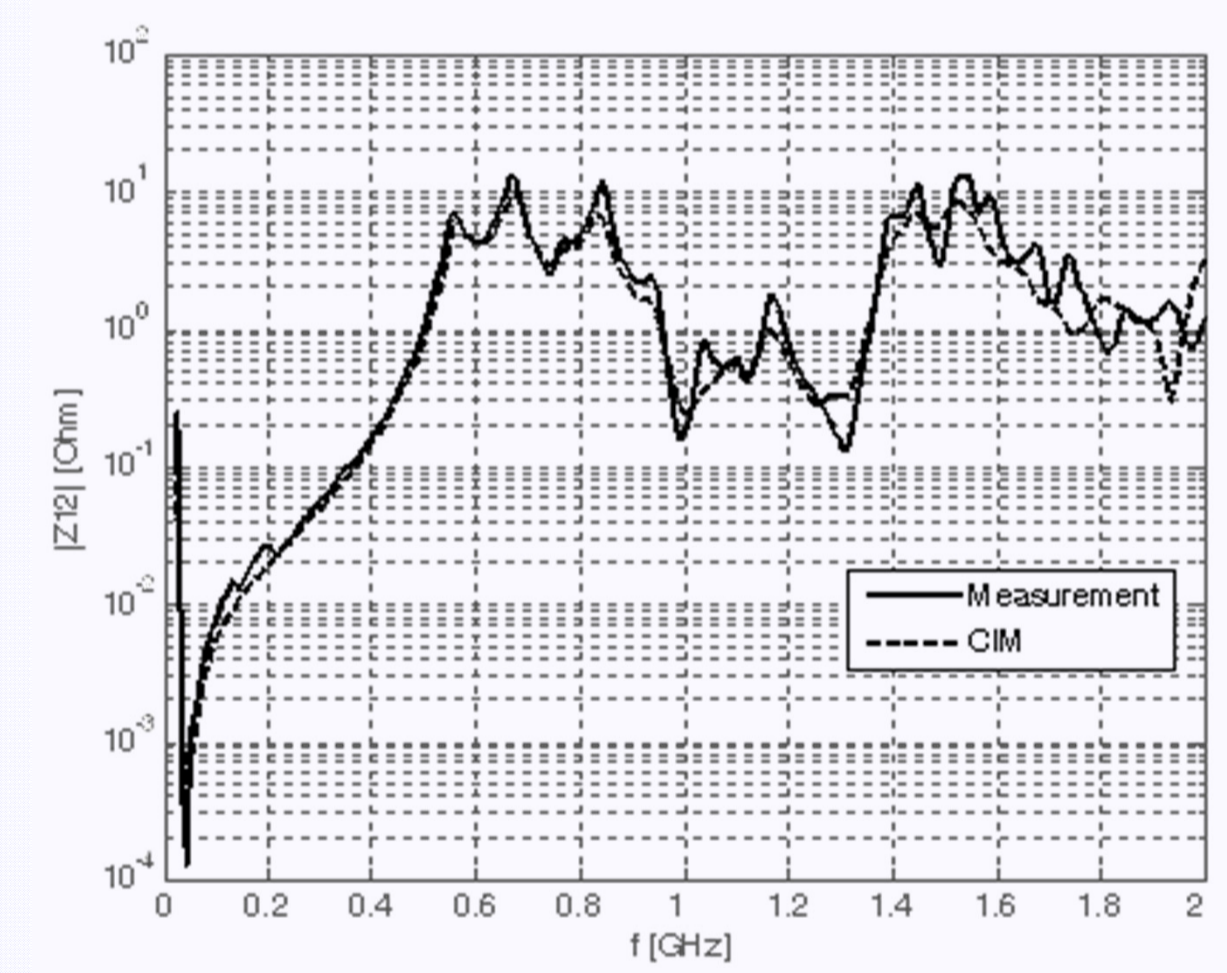
Test board with SMD decoupling capacitors



Circuit-level simulation of populated PCB



Input impedance at one port



Transfer impedance between two ports

Conclusion

- Numerically efficient and versatile EMC-analysis tool for power-bus structures in PCBs has been developed, implemented and experimentally validated. It allows
 - rapid N-port characterisation for circuit-level simulation
 - calculation of radiated fields